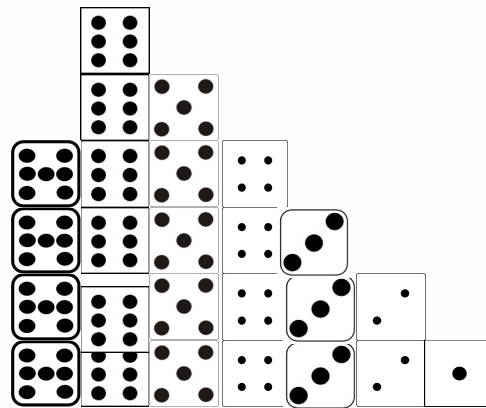


Variations of the stellar initial mass function in and between galaxies

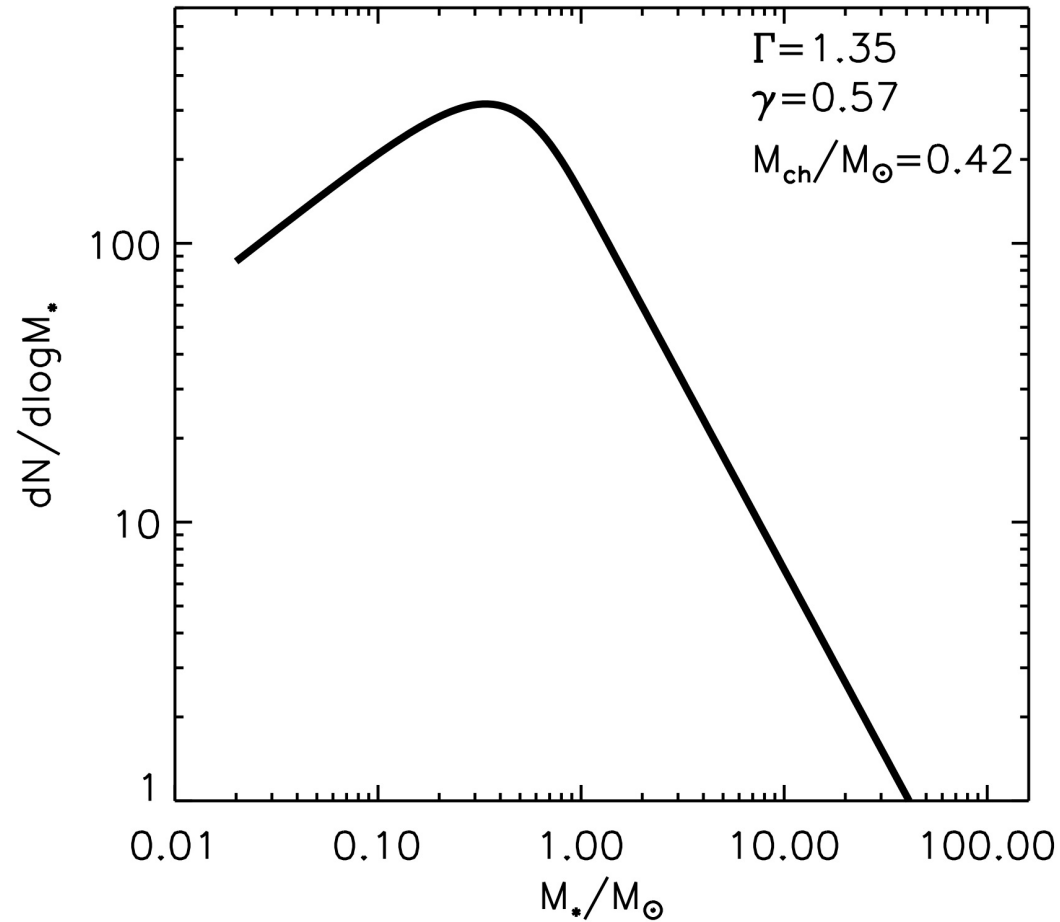
Sami Dib
MPIA, Heidelberg



IMF clusters \neq IGIMF (galactic) \neq PDMF (galactic)

PDMF-The Galactic field

The local PDMF of the MW



$$\xi(\log M) = kM^{-\Gamma} \left\{ 1 - \exp \left[- \left(\frac{M}{M_{ch}} \right)^{\gamma + \Gamma} \right] \right\}$$

A time averaged Galactic IMF

SFR → decaying exponential
 Rybizki & Just (2015)
 Mor et al. (2017, 2018)
 Sollima et al. (2019)

Mor et al. (2019): inferred both the shape of the time-averaged IMF, and of the SFH

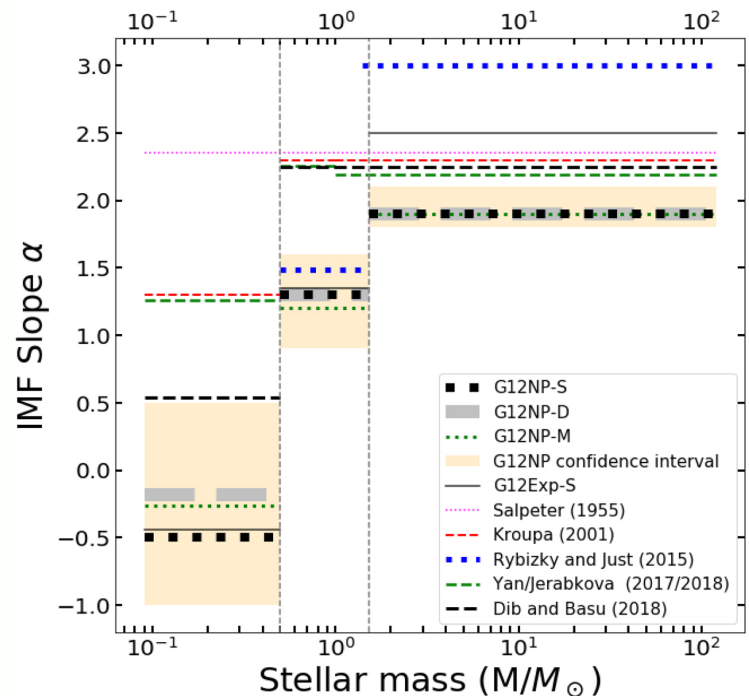
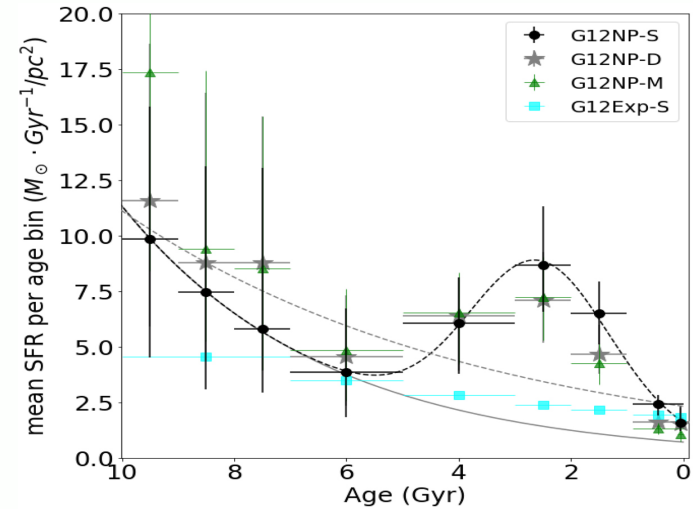
BGM models

GAIA (structure & dynamics)



Apogee (chemical composition)

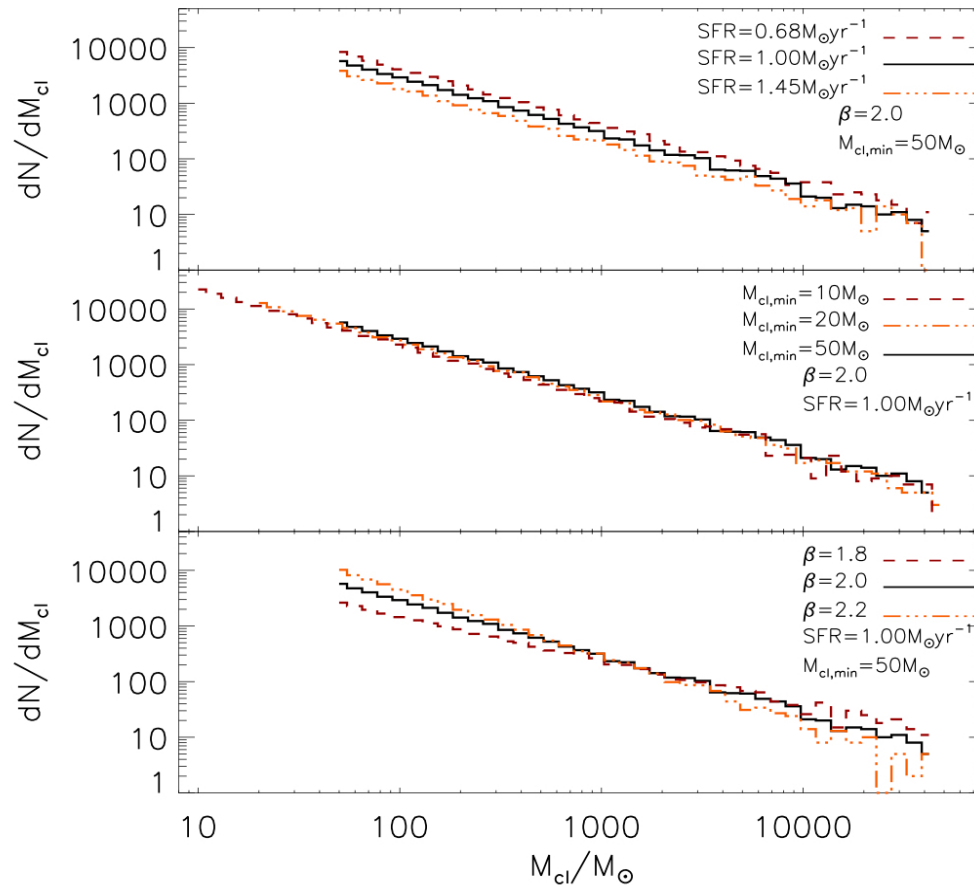
Dib & Basu (2018)



Clusters

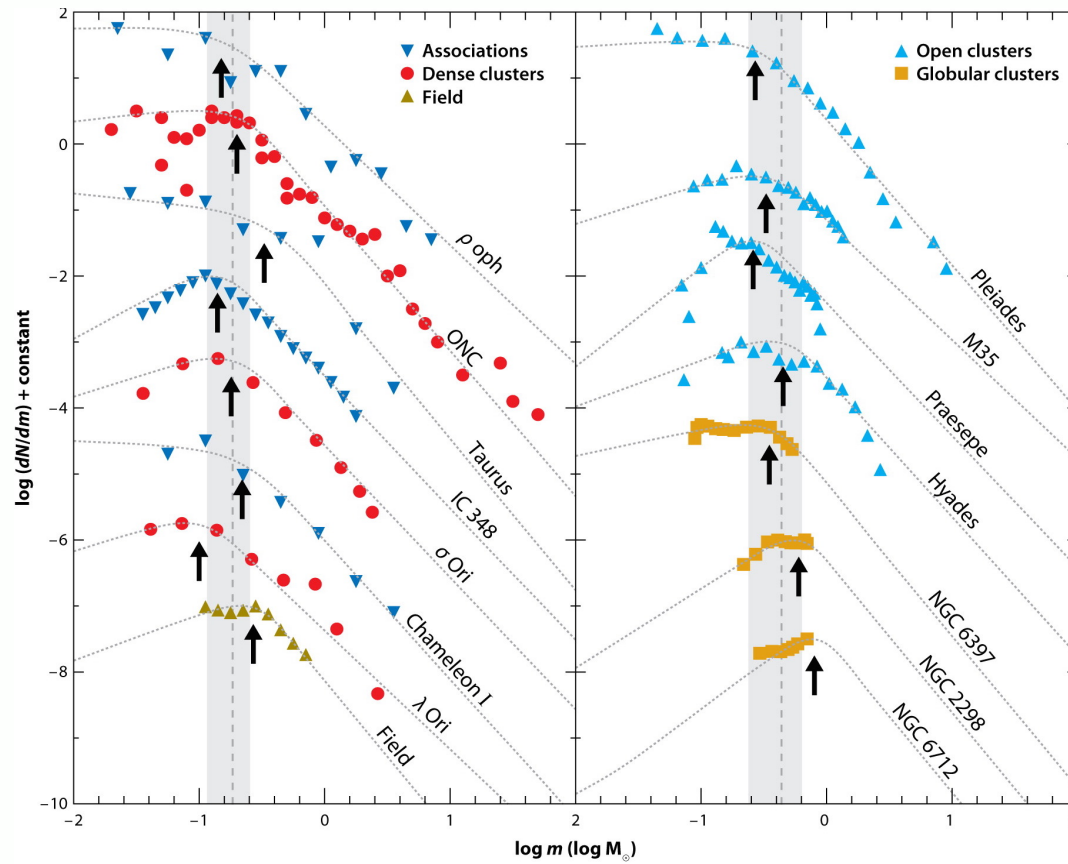
Statistics matters

The Milky Way forms $\sim 10^4$ - 10^5 clusters every 10-12 Myrs.



Dib et al. (2017)

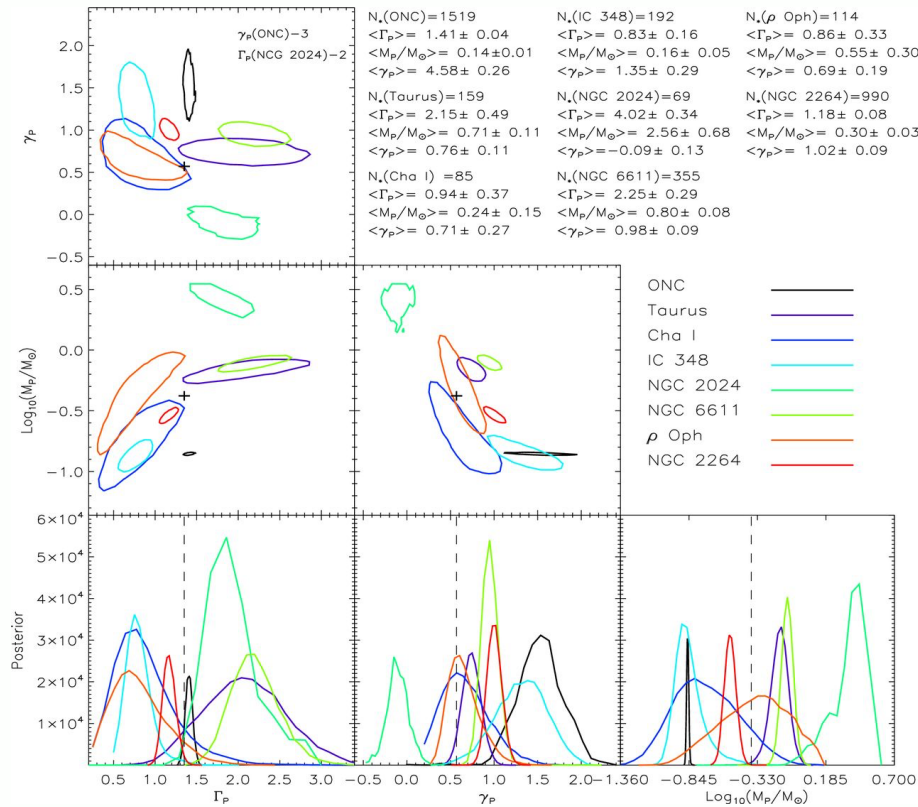
The IMF of stellar clusters



Bastian et al. (2010)

The IMF of stellar clusters

Evidence against universality



$$\xi(\log M) = kM^{-\Gamma} \left\{ 1 - \exp \left[- \left(\frac{M}{M_{ch}} \right)^{\gamma + \Gamma} \right] \right\}$$

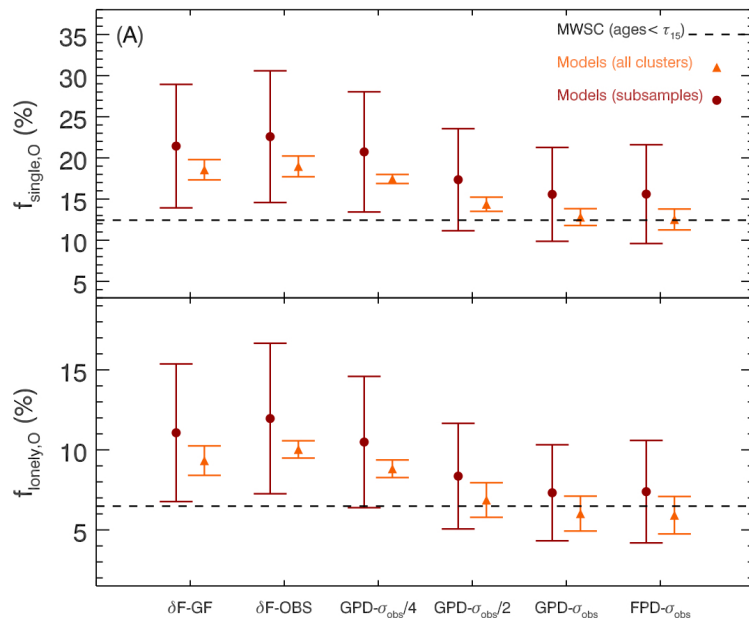
Dib 2014

The IMF of stellar clusters

Evidence against universality

Increasing width in parameter distributions

$$\sigma_{IMF} = (\sigma_{\Gamma_P} = 0.6, \sigma_{\gamma_P} = 0.25, \sigma_{M_P} = 0.27)$$



Dib+ (2017)

Libraries of synthetic clusters

- Random sample cluster masses from an ICLMF
- Random sample an age for each cluster (from the age distrib. of observed clusters)
- Random sample stellar masses in each cluster (system stellar masses)
- assign a binarity probability for each cluster
- assign a mass ratio for each binary
- Correct for stellar evolution (i.e., remove evolved O stars at the assigned age of the cluster)
- Correct for ejected O stars
- Correct the total sample for completeness (based on the B stars content)

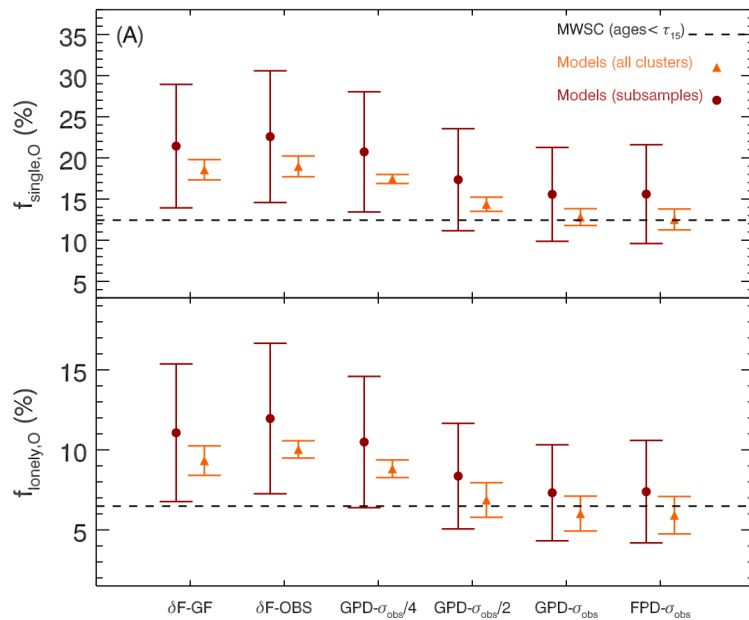
→ Measure the fractions of single and lonely O stars

The IMF of stellar clusters

Evidence against universality

Increasing width in parameter distributions

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Dib+ (2017)

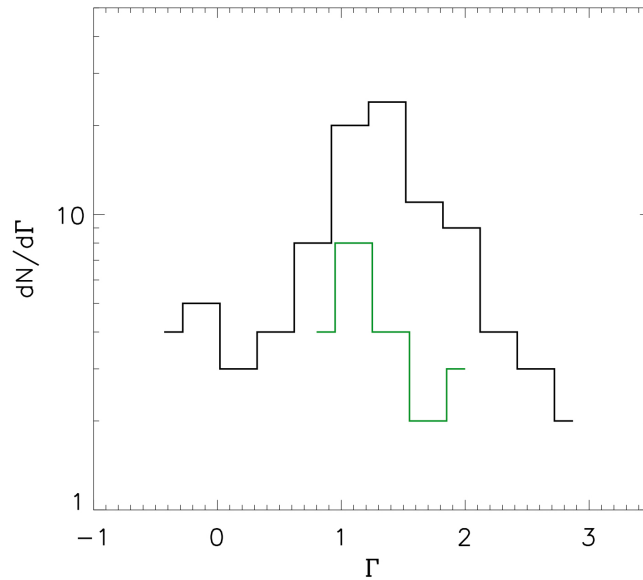
Libraries of synthetic clusters

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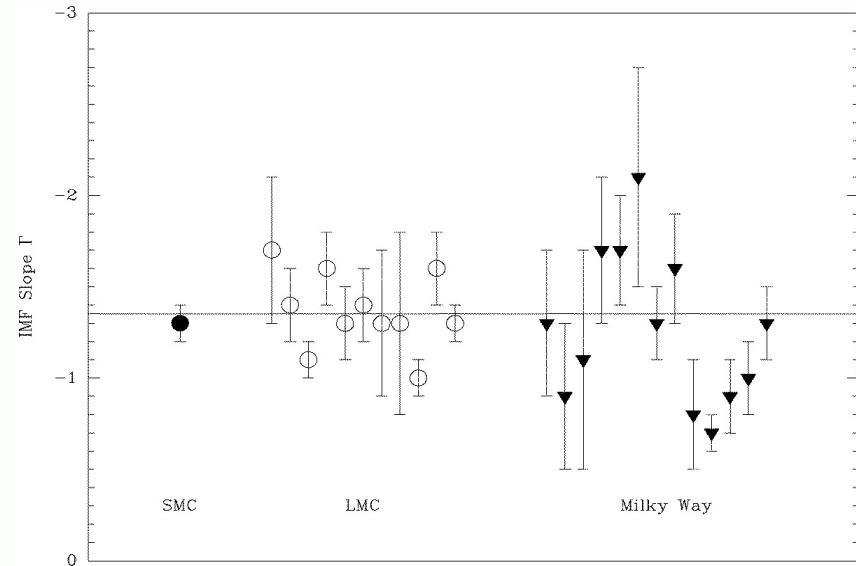
→ Measure the fractions of single and lonely O stars

The IMF of stellar clusters

Evidence against universality



**Lim et al. (2015),
Weisz et al. (2015)
Dib (in prep)**



Massey 2003

The IGIMF- galaxy-wide IMF

The galaxy-integrated IMF: IGIMF

$$\Phi_{IGIMF}(M_*) = \int_0^{\infty} \varphi_{IMF}(M_*) \zeta(M_{cl}) dM_{cl}$$

Weidner & Kroupa (2004),
++ several papers by Kroupa's group

The galaxy-integrated IMF: IGIMF

$$\Phi_{IGIMF}(M_*, SFR, [Fe/H]) = \int_{M_{cl, \min}}^{M_{cl, \max}(SFR)} \varphi_{IMF}(M_*, [Fe/H]) \zeta(M_{cl}, SFR) dM_{cl}$$

SFR dependence: $M_{cl, \max} = F(SFR)$

Metallicity dependence:
 $\Gamma = G([Fe/H])$
 $\gamma = H([Fe/H])$

The galaxy-integrated IMF with IMF variations

$$\Phi_{IGIMF}(M_*, SFR, [Fe/H]) = \int_{M_{cl,min}}^{M_{cl,max}(SFR)} \int_{\Gamma_{min}}^{\Gamma_{max}} \int_{\gamma_{min}}^{\gamma_{max}} \int_{M_{ch,min}}^{M_{ch,max}} P(M_{ch}) P(\gamma) P(\Gamma) \varphi_{IMF}(M_*, [Fe/H]) \zeta(M_{cl}, SFR) dM_{cl} d\Gamma d\gamma$$

SFR dependence: $M_{cl,max} = F(SFR)$

SFR dependence: $M_{ch} = I(SFR)$



Inspired from simulations of
Narayanan, Dave ++
(2012, 2013)

Metallicity dependence:

$$\Gamma = G([Fe/H])$$

$$\gamma = H([Fe/H])$$

Dib & Basu (2018)

Dib (2022)

IMF parameter distributions – Gaussian functions

$$P(\gamma) = \frac{1}{\sigma_\gamma \sqrt{2\pi}} \exp\left(-\frac{1}{2} \left(\frac{\gamma - \bar{\gamma}}{\sigma_\gamma}\right)^2\right)$$

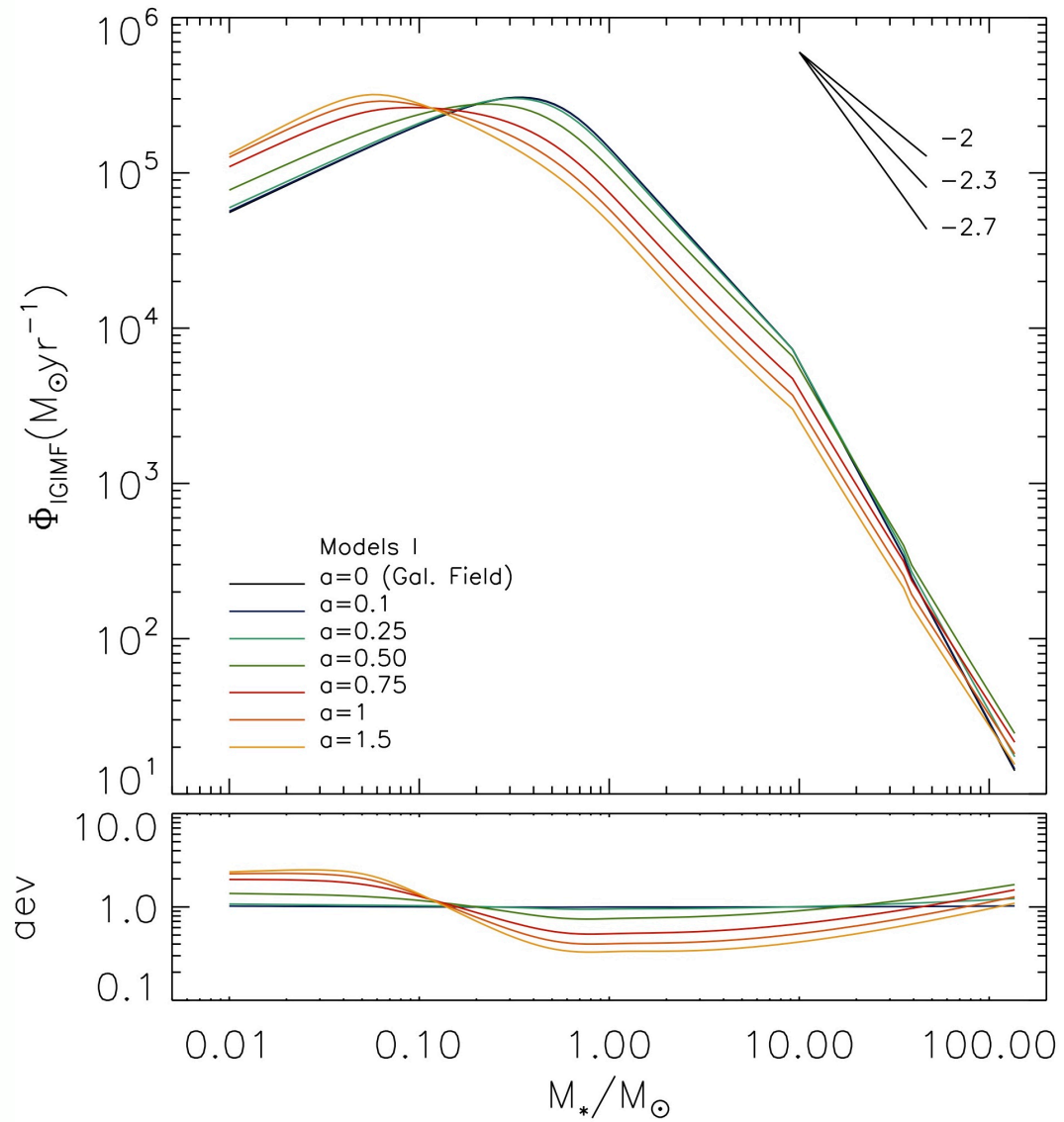
$$P(\Gamma) = \frac{1}{\sigma_\Gamma \sqrt{2\pi}} \exp\left(-\frac{1}{2} \left(\frac{\Gamma - \bar{\Gamma}}{\sigma_\Gamma}\right)^2\right)$$

$$P(M_{ch}) = \frac{1}{\sigma_{M_{ch}} \sqrt{2\pi}} \exp\left(-\frac{1}{2} \left(\frac{M_{ch} - \bar{M}_{ch}}{\sigma_{M_{ch}}}\right)^2\right)$$

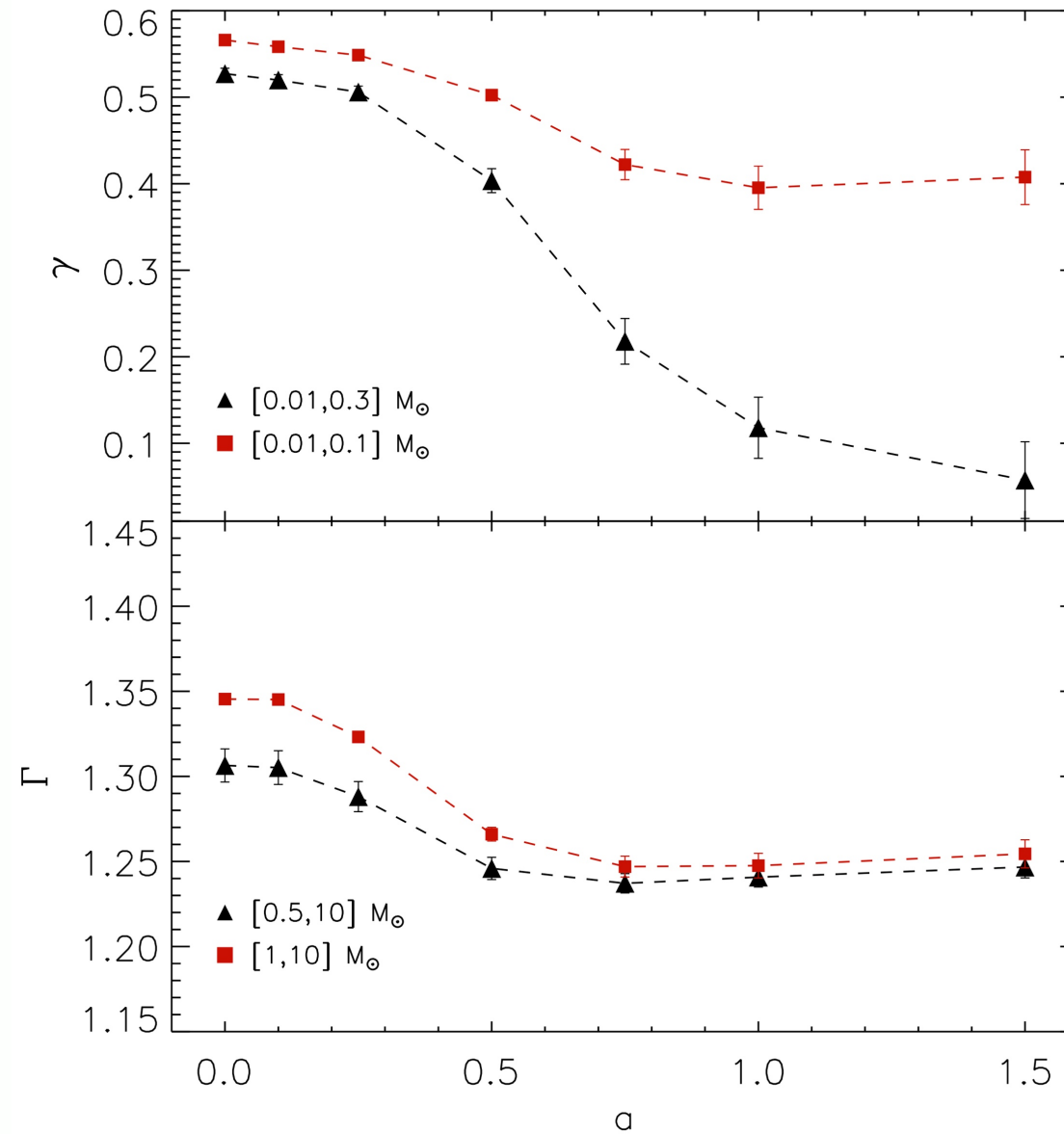
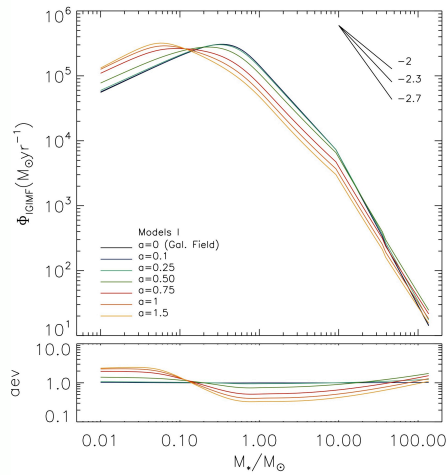
$$\sigma_\Gamma = a_\Gamma \sigma_{obs,\Gamma} \quad \sigma_\gamma = a_\gamma \sigma_{obs,\gamma} \quad \sigma_{M_{ch}} = a_{M_{ch}} \sigma_{obs,M_{ch}}$$

For simplicity, vary the a(s) in $a_\gamma = a_\Gamma = a_{M_{ch}} = a$
unison:

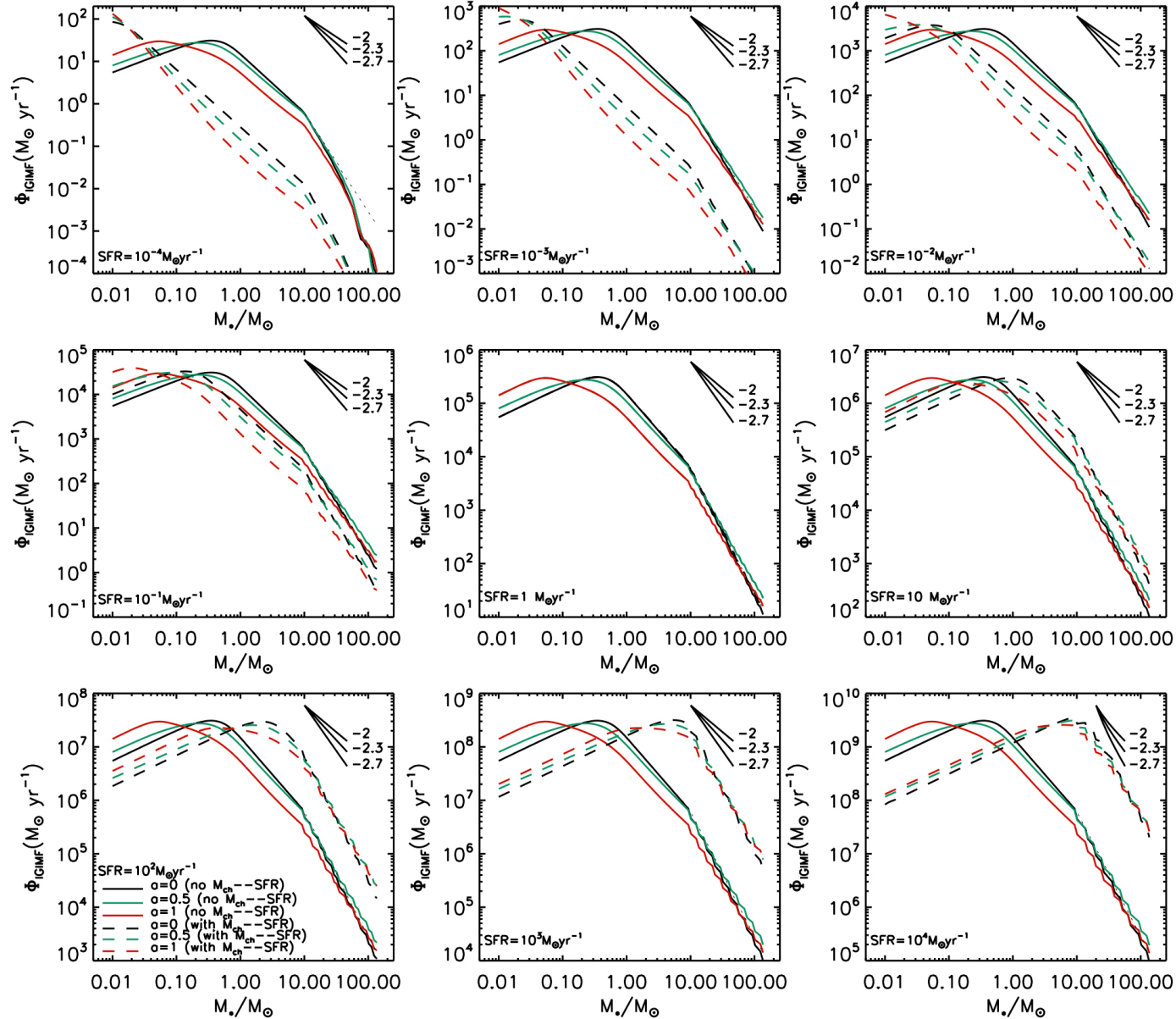
Effects of IMF variations in clusters on the IGIMF



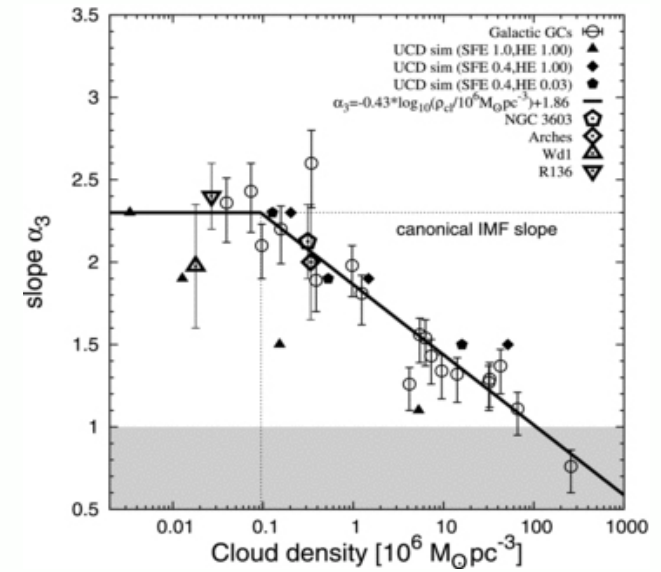
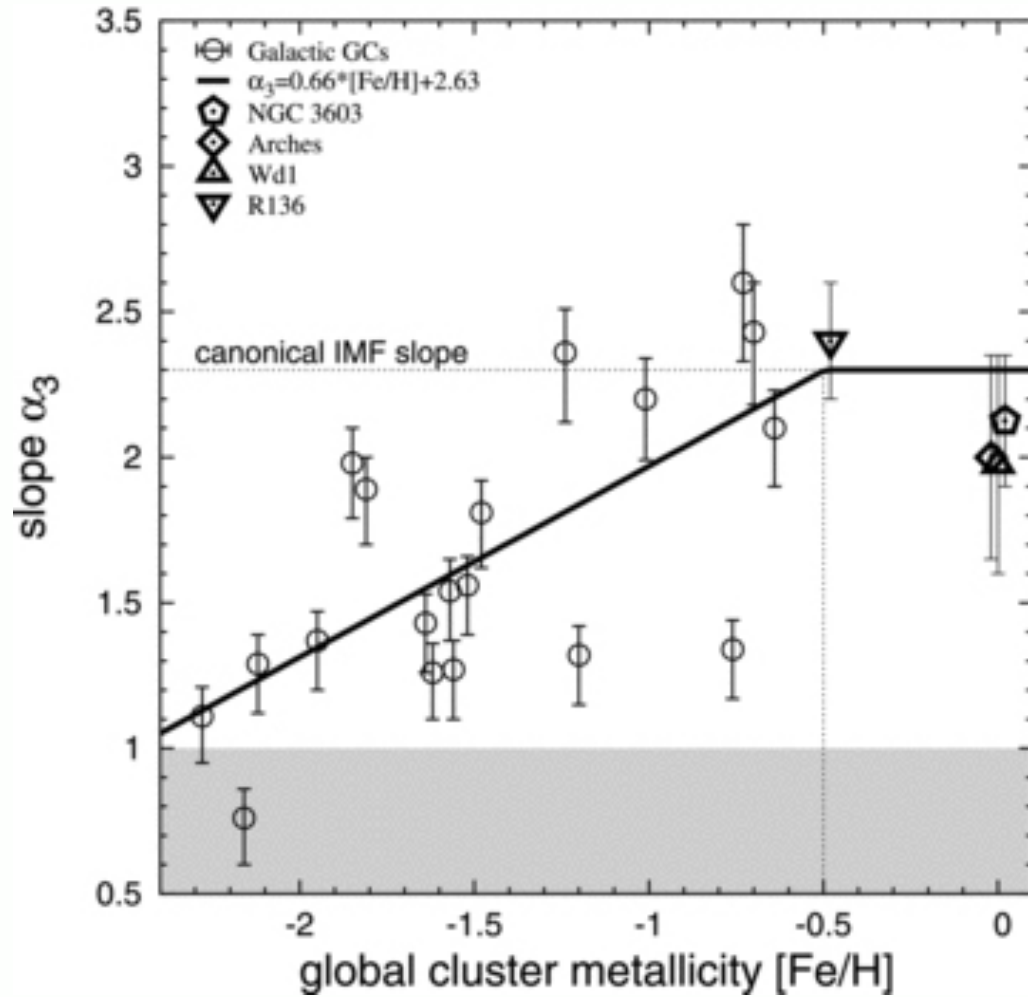
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Effects of IMF variations in clusters on the IGIMF

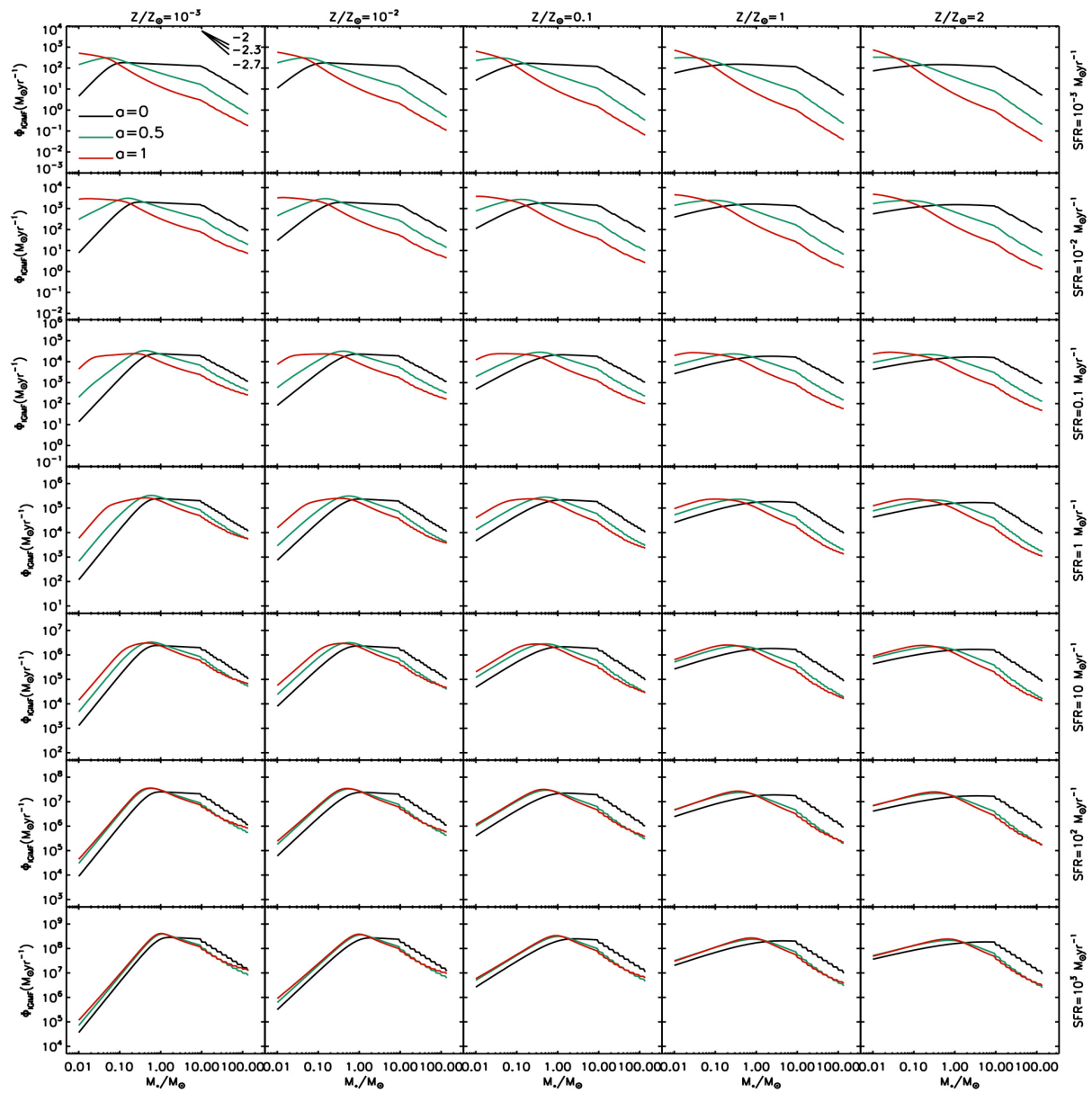


Metallicity dependence

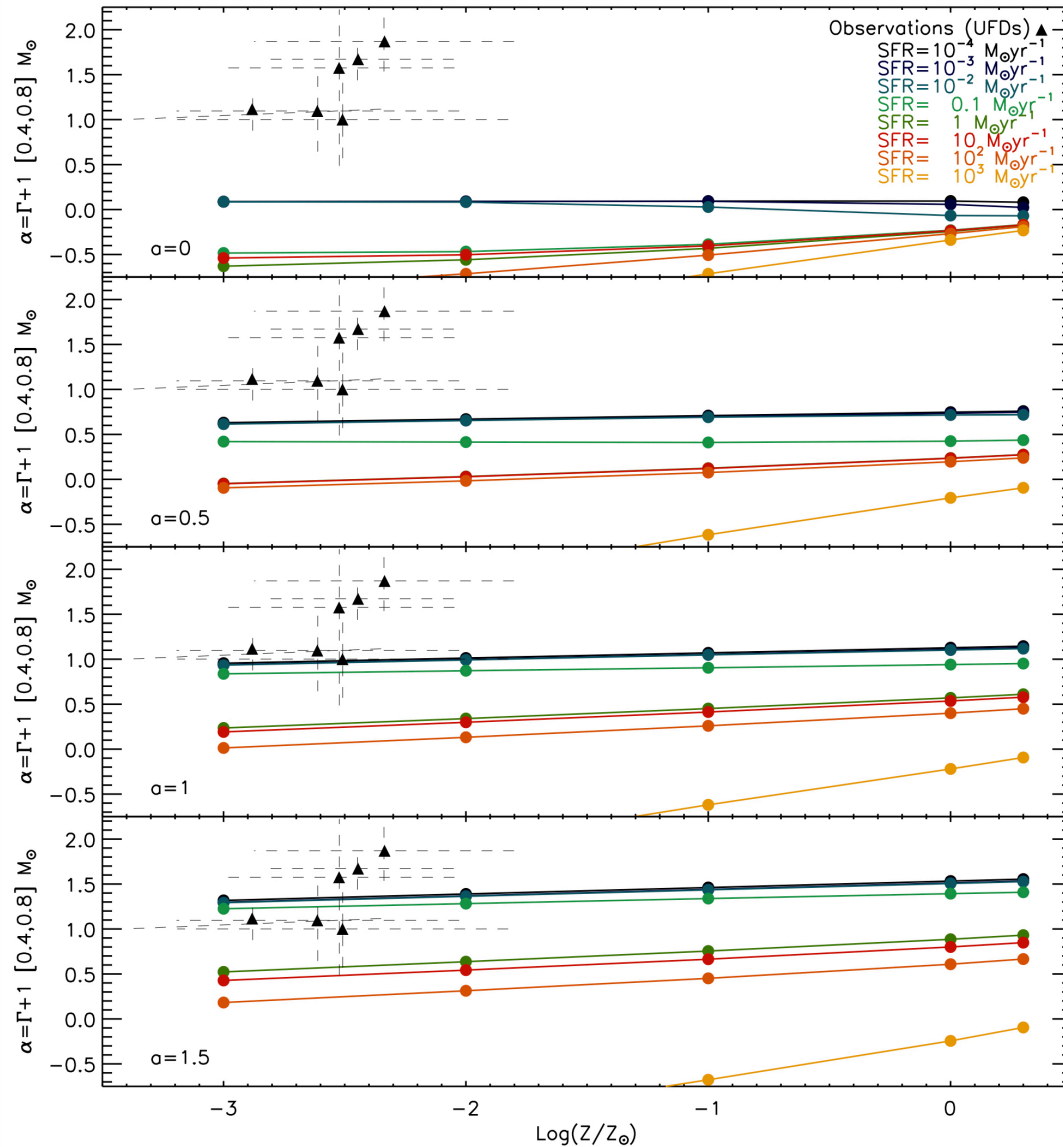


Marks et al. (2012)

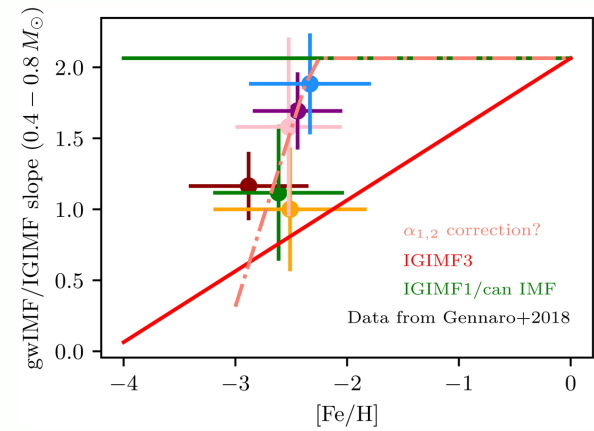
Grid in Metallicity-SFR



Comparison to observations - UFDs



Dib (2022)



Jerabkoba+ 18

Some conclusions

- Variations of the IMF in Galactic clusters
 - Level of variation $\sigma_{IMF} = (\sigma_{\Gamma_p} = 0.6, \sigma_{\gamma_p} = 0.25, \sigma_{M_p} = 0.27)$
 - Necessity to measure variations in and outside the MW
- Accounting for IMF variation is necessary to fit the IGIMF/PDMF of Ultra-faint dwarfs ...and probably for all galaxies at all epochs
- Should have consequences for gas dynamics and chemical enrichment
- Next step: calculate galactic PDMFs